

## Linear Programming

### Homework Set # 7

Due in class on Tuesday, November 15, 2011.

2). A company produces and sells wooden soldiers and wooden trains. Each soldier requires 3 board feet of lumber and 2 hours of labor. Each train requires 5 board feet of lumber and 4 hours of labor. A total of 145 board feet of lumber and 90 hours of labor are available. Upto 50 soldiers and 50 trains can be sold. Trains sell for \$55, and soldiers for \$32. In addition to producing trains and soldiers itself, the company can buy (from an outside supplier) extra soldiers at \$27 each and extra trains at \$50 each. Let  $SM, TM$  be the number of soldiers and trains made by the company, and  $SB, TB$  the number of soldiers and trains bought from the supplier. Use the Lindo output on the next page to answer each of the following parts.

- (a). If the company can purchase trains for \$48, what would be the new optimal profit?
- (b). What is the most that the company should be willing to pay to for another board foot of lumber?
- (c). If only 40 trains could be sold, what would be the new optimal solution (the  $z$ )?
- (d). If only 40 trains could be sold, and 91 hours of labor are available, what would be the new optimal solution (the  $z$ )?
- (e). The company is considering producing sets of wooden blocks. Demand for blocks is unlimited. Each set of wooden blocks requires 10 board feet of lumber and 1 hour of labor, and sells for \$20. Should the company produce any blocks?

max	$32SM + 55TM + 5SB + 5TB$	
s.t. 2)	$3SM + 5TM$	$\leq 145$
3)	$2SM + 4TM$	$\leq 90$
4)	$SM + SB$	$\leq 50$
5)	$TM + TB$	$\leq 50$
	objective function value	1715.00000
	variable	value
	$SM$	45.000000
	$TM$	.000000
	$SB$	5.000000
	$TB$	50.000000
	row	slack or surplus
	2)	10.000000
	3)	.000000
	4)	.000000
	5)	.000000
		dual prices
	2)	0.000000
	3)	13.500000
	4)	5.000000
	5)	5.000000

Range in which basis remains unchanged :

OBJ coefficient ranges

variable	current coef	allowable increase	allowable decrease
$SM$	32.000000	infinity	2.00000
$TM$	55.000000	4.00000	infinity
$SB$	5.00000	2.00000	5.00000
$TB$	5.00000	infinity	4.00000

righthand side ranges

row	current RHS	allowable increase	allowable decrease
2	145.00000	infinity	10.000000
3	90.00000	6.66667	90.00000
4	50.00000	infinity	5.00000
5	50.00000	infinity	50.00000

3). Consider the following problem and the accompanying optimal tableau ( $x_4, x_5$  are the respective slack variables):

$$\begin{aligned} \max \quad & z = 2x_1 + x_2 - x_3 \\ \text{s.t.} \quad & x_1 + 2x_2 + x_3 \leq 8 \end{aligned}$$

$$\begin{aligned}
 -x_1 + x_2 - 2x_3 &\leq 4 \\
 x_1, x_2, x_3 &\geq 0
 \end{aligned}$$

	$z$	$x_1$	$x_2$	$x_3$	$x_4$	$x_5$	RHS
$z$	1	0	3	3	2	0	16
$x_1$	0	1	2	1	1	0	8
$x_5$	0	0	3	-1	1	1	12

- (a). Suppose the coefficient of  $x_2$  in the objective function is changed from 1 to 3.5. Use sensitivity analysis to find the new optimal solution.
- (b). Suppose that constraint  $x_2 + x_3 = 3$  is added to the problem. Use sensitivity analysis to find the new optimal solution.
- (c). Suppose that a new activity,  $x_6$ , is proposed with unit return  $c_6 = 4$  and consumption vector  $a_6 = (1, 2)^t$ . Use sensitivity analysis to find the new optimal solution.