

## Answer for 7.56 (pg. 258)

**7.56.**  $H_0 : \mu = \mu_0 = 200$ ,  $H_1 : \mu \neq 200$ .

$\sigma = 20$ ,  $n = 8$ ,  $\alpha = 0.05$ . Note use normal test.

Type II error is

$$\begin{aligned}\beta(\mu) &= P\{\text{accepting } H_0 \text{ when } H_1 \text{ is true}\} \\ &= P\left\{-z_{\alpha/2} < \frac{\bar{X} - \mu_0}{\sigma/\sqrt{n}} < z_{\alpha/2}\right\} \\ &= P\left\{-z_{\alpha/2} + \frac{\mu_0 - \mu}{\sigma/\sqrt{n}} < \frac{\bar{X} - \mu}{\sigma/\sqrt{n}} < z_{\alpha/2} + \frac{\mu_0 - \mu}{\sigma/\sqrt{n}}\right\} \\ &= F\left(z_{\alpha/2} + \frac{\mu_0 - \mu}{\sigma/\sqrt{n}}\right) - F\left(-z_{\alpha/2} + \frac{\mu_0 - \mu}{\sigma/\sqrt{n}}\right) \\ &= F\left(1.96 + \frac{200 - \mu}{20/\sqrt{8}}\right) - F\left(-1.96 + \frac{200 - \mu}{20/\sqrt{8}}\right)\end{aligned}$$

$$\beta(190) = 0.7.$$